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METHOD OF PROCESSING AN ANALOG SIGNAL AND DEVICE FOR  
IMPLEMENTING THE METHOD

The invention relates to a method of processing an  
5 analog signal whose frequency spectrum exhibits over a  
determined bandwidth two main lobes separated by a  
frequency band where the power is negligible.

A subject of the invention is also a device for  
10 processing a corresponding analog signal.

The field of the invention is that of satellite based  
radionavigation.

15 Current radionavigation systems such as the GPS,  
GLONASS systems, are systems for positioning in three  
dimensions, based on the reception of signals  
transmitted by a constellation of satellites.

20 The signal transmitted by a satellite is typically  
composed of a carrier modulated with a spreading code  
and possibly data; BPSK modulation (the acronym  
standing for Binary Phase Shift Keying) which gives a  
carrier exhibiting phase jumps of  $\pi$  on each change of  
25 the binary code, is commonly used in current systems.

Represented in Figure 1a is a carrier of period T, a  
random binary spreading code of frequency  $F_{code}$ , the  
resulting signal, modulated according to a BPSK  
30 modulation (designated the BPSK signal for simplicity)  
and the envelope of the corresponding frequency  
spectrum. The frequency spectrum of a BPSK signal has  
(in terms of power) an envelope of the form

$1/F_{code} \cdot \text{sinc}^2(|f-f_p|/F_{code})$  with  $\text{sinc } x = \frac{\sin \pi x}{\pi x}$  which

35 exhibits two unique main lobes centered respectively on  
the carrier frequency  $f_p$  ( $f_p=1/T$ ), and the frequency  $-f_p$   
of the adjacent sidelobes.

In order to improve the navigation performance such as the accuracy of the positioning, the resistance to jamming, ..., the new satellite based navigation systems (improved GPS, Galileo, use BOC modulation (the acronym standing for Binary Offset Carrier). Represented in Figure 1b is the signal resulting from the same carrier and from the same spreading code, but this time modulated according to a BOC modulation (designated BOC signal for simplicity), and the envelope (in terms of power) of the corresponding frequency spectrum, which is of the form

$$1/F_{\text{code}} \cdot \text{sinc}^2(|f-f_p|/F_{\text{code}}) \cdot \sin^2(\pi|f-f_p|/2f_{\text{sp}}) / \cos^2(\pi|f-f_p|/2f_{\text{sp}}).$$

The frequency spectrum of a BOC signal exhibits two identical main lobes spaced either side of  $f_p$  (respectively  $-f_p$ ), with each of the adjacent sidelobes, as represented in Figure 1b. The BOC modulation may be regarded as being a BPSK modulation applied after having previously multiplied the carrier by a subcarrier whose frequency  $f_{\text{sp}}$  is often a multiple of  $f_p$ .

The signal transmitted by the satellite is an analog signal which, after having traversed the distance between the satellite and the receiver, is converted by the receiver into a digital signal with a view to subsequent digital processing. This conversion comprises a step of sampling the spectrum of the signal received by the receiver, followed by a digitizing step. The sampling is carried out according to a sampling frequency  $f_e$ . It is known that in order to comply with Shannon's criterion which makes it possible to avoid spectral aliasing, the sampling frequency  $f_e$  must be greater than or equal to the bandwidth of the spectrum.

Now, the spectrum of a BOC signal, whose lobes are spaced apart, has a wider frequency band than that of a BPSK signal, as illustrated in Figures 1a) and 1b): as

a result, the sampling of a BOC signal is carried out according to a higher sampling frequency than that of a BPSK signal. Now, the use of a high sampling frequency has the drawback of inducing extra cost and an increase  
5 in consumption.

A solution for alleviating this drawback consists in processing only part of the spectrum after analog filtering: this makes it possible to reduce the  
10 frequency band before sampling. However, it results in a loss of power of the digital signal obtained and a loss of accuracy in the position.

An important aim of the invention is therefore to  
15 preserve the advantages related to BOC modulation while reducing the sampling frequency.

To achieve these aims, the invention proposes a method of processing an analog signal whose frequency spectrum  
20 exhibits over a determined bandwidth two main lobes separated by a frequency band where the power is negligible, chiefly characterized in that it comprises a step of sampling according to a determined sampling frequency, and prior to this sampling step, a step  
25 consisting in performing a frequency translation of the two main lobes towards one another with a view to reducing the bandwidth and hence the sampling frequency.

30 This translation may be obtained by two procedures.

The step of translating the lobes may be obtained by multiplying the analog signal by a signal of the type  $\cos(\omega t)$ ,  $\omega$  being determined as a function of the  
35 subcarrier frequency and of the bandwidth of the main lobes; the translation of the main lobes having generated spurious lobes, the method furthermore comprises, prior to the sampling, a step of filtering

the translated lobes, with a view to eliminating the spurious lobes.

5 The translation of the lobes and the sampling may be grouped together into a single step consisting in sampling the analog signal according to a specific sampling frequency  $f_{es}$ ; the analog signal having been modulated by a carrier and a subcarrier of frequency  $f_{sp}$ , the frequency  $f_{es}$  is related to the frequency  $f_{sp}$  by  
10 the following relation  $f_{sp} = N.f_{es} - f_{es}/4$ ,  $N$  being a determined integer greater than or equal to 1.

It preferably comprises a prior step of converting the analog signal to baseband.

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The analog signal may be a signal modulated according to a BOC type modulation.

20 According to a characteristic of the invention, the BOC signal comprising a carrier, a code and a subcarrier, respectively exhibiting determined frequencies, the method comprises a step of digitizing the sampled signal and a step of demodulating the digitized signal based on the use of a code and of a subcarrier that are  
25 generated locally, the local code being generated on the basis of the frequency of the code, the local subcarrier being generated on the basis of the frequency of the subcarrier determined and reduced during the step of translating the lobes.

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The analog signal is a radionavigation signal.

35 A subject of the invention is also a device for processing an analog signal whose frequency spectrum exhibits over a determined bandwidth two main lobes separated by a frequency band where the power is negligible, characterized in that it comprises an element for translating the frequency of the main lobes

towards one another which is able to reduce the bandwidth.

The invention finally relates to a receiver of a  
5 radionavigation system comprising such a device.

Other characteristics and advantages of the invention will become apparent on reading the detailed description which follows, offered by way of  
10 nonlimiting example and with reference to the appended drawings, in which:

Figure 1a) diagrammatically represents a carrier of period  $T$ , a random binary spreading code equal to 1,  
15 -1, 1, 1, ..., and the resulting BPSK signal transmitted, expressed as a function of time and the envelope of the corresponding frequency spectrum, expressed in terms of power,

20 Figure 1b) diagrammatically represents the same code and carrier as those of Figure 1a) as well as a subcarrier and the product of the code times this subcarrier expressed as a function of time and the envelope of the corresponding frequency spectrum,  
25 expressed in terms of power,

Figures 2a), 2b) and 2c) diagrammatically represent the envelopes of the frequency spectra (expressed in terms of power) of the BOC signal of Figure 1b), at the  
30 output of the antenna of the receiver (Figure 2a), after its conversion to intermediate frequency  $F_i$  (Fig 2b) and baseband (Fig 2c),

Figures 3a), 3b) and 3c) diagrammatically represent  
35 (expressed in terms of power) the envelope of the frequency spectrum of the BOC signal of Figure 2c) after filtering (Figure 3a), the frequency spectrum of a  $\cos(\omega t)$  signal (Figure 2b) and the envelope of the frequency spectrum of the BOC signal of Figure 3a whose

lobes have undergone a translation by an analog procedure (Figure 3c),

Figures 4a) and 4b) diagrammatically represent  
5 (expressed in terms of power) the envelope of the frequency spectrum of the BOC signal of Figure 2c) after filtering (Fig 4a) and the envelope of the frequency spectrum of the BOC signal of Figure 4a whose lobes have undergone a translation by a digital  
10 procedure (Figure 4b),

Figure 5 diagrammatically represents a first embodiment of a device for processing an analog signal according to the invention,

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Figure 6 diagrammatically represents a second embodiment of a device for processing an analog signal according to the invention,

20 Figure 7 diagrammatically represents the feedback loop for slaving the carrier and slaving the code and the subcarrier in the case of a device for processing a conventional BOC signal,

25 Figure 8 diagrammatically represents an element for calculating the local phase common to the code generator and the subcarrier generator in the case of a device for processing a conventional BOC signal,

30 Figure 9a) and 9b) diagrammatically represent the local code (Fig 9a) and the local subcarrier (Fig 9b) as a function of the local phases expressed in terms of chips, in the case of a device for processing a conventional BOC signal,

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Figure 10 diagrammatically represents the feedback loop for slaving the carrier and for slaving the code and the subcarrier in the case of a device for processing a BOC signal according to the invention,

Figure 11 diagrammatically represents an element for calculating the phase of the local code and an element for calculating the phase of the local subcarrier in the case of a device for processing a BOC signal according to the invention,

Figures 12a) and 12b) diagrammatically represent the local code (Fig 12a) as a function of the local phase expressed in terms of chips and the local subcarrier (Fig 12b) as a function of the local phase expressed in cycles, in the case of a device for processing a BOC signal according to the invention.

A BOC signal will now be more particularly considered. The method according to the invention aims to reduce the sampling frequency of a BOC signal.

At the output of the antenna of the receiver, the BOC signal is, in a conventional manner, converted into baseband, possibly passing through a prior conversion to intermediate frequency  $F_i$ . A bandpass filtering is generally applied before the conversion (or conversions) so as to eliminate certain sidelobes; a low-pass filtering is generally applied after the conversion(s).

Represented is the spectrum of the BOC signal of Figure 1b at the output of the antenna of the receiver (Fig 2a), after its conversion to intermediate frequency  $F_i$  (Fig 2b) then to baseband (Fig 2c). The bandwidth of the spectrum is then  $B_{\text{initial}}$  or  $B_i$ . The BOC signal after its conversion to intermediate frequency  $F_i$  is a real signal whereas after its conversion to baseband, the signal which comprises a channel I and a channel Q (in quadrature with respect to the I channel), is complex.

Thereafter, the sidelobes of the frequency band situated between the two main lobes are preferably eliminated by filtering so as to avoid aliasing during sampling. The width of the band containing at least one  
5 main lobe is designated  $B_{lobe}$ , or  $B_1$ .

We saw that in order to comply with Shannon's criterion, the sampling frequency  $f_e$  is greater than or equal to the bandwidth of the spectrum of the BOC  
10 signal, in this instance  $B_1$ .

It is therefore possible to reduce  $f_e$  by reducing the bandwidth, prior to sampling. To do this, the bandwidth of the spectrum of the BOC signal is reduced by  
15 performing a frequency translation of the two main lobes towards one another. This translation may be obtained by two procedures.

A first, analog procedure consists in multiplying the I and Q channels by a signal in  $\cos(\omega t)$  represented in  
20 Figure 3b,  $\omega$  being of the form  $2\pi(f_{sp}-f_{spred})$ . The spectra before and after multiplication are respectively represented in Figures 3a and 3c; after multiplication, each lobe is then centered on a reduced subcarrier  
25 frequency,  $f_{spred}$ . We have  $f_{spred} \geq B_1/2$ . A last filtering makes it possible to eliminate the spurious lobes so as to avoid aliasing during sampling.

One then obtains a spectrum consisting of two main  
30 lobes having undergone a translation towards one another and whose bandwidth is equal to around  $2B_1$  as illustrated in Figure 3c; the spectrum is then sampled according to a sampling frequency  $f_e$  greater than or equal to  $2B_1$ .

35 Another, digital, procedure makes it possible at one and the same time to perform a translation of the main lobes towards one another and to sample: this is obtained by performing a sampling according to a



specific sampling frequency  $f_{es}$ . This frequency  $f_{es}$  is determined on the basis of the following conditions, aimed at avoiding any overlap between lobes during this specific sampling.

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- (1)  $f_{es}$  must be greater than or equal to  $2B_l$ ,
- (2)  $f_{sp} + B/2 < N \cdot f_{es}$ ,  $N$  being an integer greater than or equal to 1
- (3)  $(N - 1/2) f_{es} < f_{sp} - B/2$

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These conditions are illustrated in Figures 4a and 4b, in which are respectively represented the spectrum before sampling and the spectrum after sampling as desired, that is to say without overlapping of lobes.

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More particularly represented in Figure 4b are the first and second main lobes corresponding to the spectral line situated at the frequency 0: to comply with the nonoverlap condition, the frequency band of this first lobe must be situated short of the frequency  $N \cdot f_{es}$  and beyond the frequency  $(N - 1/2) \cdot f_{es}$ , this giving rise to conditions (1), (2) and (3).

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These conditions are fulfilled for  $f_{sp} = N \cdot f_{es} - f_{es}/4$ .

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We preferably take for  $N$  the largest value fulfilling this condition so as to minimize  $f_{es}$ .

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This digital procedure has the advantage of carrying out two steps (bringing the lobes closer together and sampling) in one and furthermore makes it possible to avoid the need to perform by an analog procedure the double multiplication by the signal  $\cos(\omega t)$ .

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A translation of the main lobes towards one another by a translation of each lobe was presented in the above examples. A translation of just one lobe towards the other also makes it possible to reduce the bandwidth and may therefore be performed according to a variant of the invention.

The method according to the invention may also be applied to "pseudo-BOC" analog signals obtained on the basis of two signals transmitted by one and the same source and synchronously, on two distinct and close frequencies, each signal being processed as a lobe of the spectrum of a BOC signal. This is for example the case for the Galileo system with signals transmitted in the frequency bands E1 and E2.

In the examples presented, the main lobes are identical, but the invention applies equally in the case where the main lobes are not.

Once sampled according to one of the procedures described previously, the analog signal is digitized. The analog signal thus converted into a digital signal is then processed as a function of the desired application.

An exemplary device for processing an analog signal included in a receiver of a positioning system, represented in Figures 5 and 6, will now be described.

At the output of the antenna 1, the analog signal whose carrier exhibits a frequency  $f_p$ , is filtered by means of a bandpass filter 2 which may be a ceramic filter. The signal is then preferably amplified by a low noise amplifier 3. At this juncture we obtain a signal whose spectrum corresponds to that of Figure 2a, that is to say riddled of certain sidelobes.

The conversion of this amplified signal to baseband is obtained by multiplying it by means of a multiplier 4 on a first channel designated the I channel by a signal of the form  $\cos(2\pi.f_p.t)$  and by means of another multiplier 4' on a second channel designated the Q channel by a signal of the form  $\sin(2\pi.f_p.t)$ . The signals of the form  $\cos(2\pi.f_p.t)$  and  $\sin(2\pi.f_p.t)$

emanate from a local oscillator 5. The spectrum of the complex signal (I and Q channel) thus obtained is of the form of that of Figure 2c.

5 On each channel, the signal thus multiplied is filtered by means of a bandpass filter 6 or 6' which may be an RC filter (comprising a resistor R and a capacitor C) or a surface wave filter (SAW filter) so as to  
10 eliminate the sidelobes of the frequency band situated between the two main lobes. The signal obtained then has a spectrum as represented in Figure 3a or 4a.

The implementation of the analog procedure is obtained by disposing as represented in Figure 5, on each I and  
15 Q channel a multiplier 7 or 7' able to multiply the signal by a signal of the form  $\cos(\omega.t)$  emanating from the local oscillator 5, then a low-pass filter 8 or 8' making it possible to eliminate the spurious lobes, as indicated in Figure 3c.

20 The signal obtained is then sampled by means of a sampler using a sampling frequency  $f_e$  greater than or equal to  $2B_l$  and digitized by means of a digitizer which produces a digital signal, these sampler and  
25 digitizer being grouped together in a converter 9 or 9'.

The implementation of the digital procedure is obtained by disposing directly as represented in Figure 6 on  
30 each I and Q channel a sampler using a sampling frequency  $f_{e_s}$  and a digitizer which produces a digital signal, this sampler and digitizer being grouped together in a converter 10 or 10'.

35 The digital processing of the signal obtained in each of the I and Q channels has then been performed according to the application desired.

The main steps of processing the digital signal in the case of a receiver positioning application based on signals of BOC type transmitted by satellites will now be described. It is recalled as indicated in the preamble that a BOC signal may be regarded as consisting mainly of a carrier, a subcarrier and a code.

In the case of a positioning application based on a conventional BOC signal, it is known to the person skilled in the art that the aim of the processing of the signal is to demodulate the digitized BOC signal into a carrier, subcarrier and code so as to recover the measure of the propagation delay on the basis of the difference between the time of transmission of the code by the satellite and the time of reception of the code by the receiver.

The demodulation is achieved by correlation of the digitized BOC signal with locally generated carrier, subcarrier and code.

These local signals must be generated synchronously with the BOC signal received, taking account in particular of the apriori unknown Doppler effect.

To do this, carrier and code tracking loops are installed, the code loop including the tracking of the subcarrier; these loops slave the phases of the local carrier, subcarrier and code with respect to the phases of the carrier, subcarrier and code of the BOC signal received, on the basis of the measurements emanating from the correlations.

The measurement of the delay in the code and the initial Doppler effect is achieved in an acquisition phase also referred to as a lockon phase which consists in testing in open loop several hypotheses regarding the position of the code and the Doppler effect until

the result of the correlation indicates through a high energy level that the phase shift between the signal received and the local signal is a minimum. Thereafter, the search is refined and then the loops are closed.

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These demodulation steps are obtained by means of a demodulator comprising feedback loops, an example of which is represented in Figure 7. In Figures 7 and 10, the digitized signal at the input of the feedback loops is as was seen previously a complex signal comprising an I channel and a Q channel.

The correlation of the signal received with the local signal is achieved firstly by multiplying by means of a multiplier 11 the digitized signal by a signal of the form  $e^{-i\varphi}$ ,  $\varphi$  being the phase of the local carrier. The signal obtained is then multiplied by means of a multiplier 12 on a so-called punctual channel (hence the notation  $I_p$  and  $Q_p$  for punctual I channel and punctual Q channel) by a signal representative of the code and subcarrier modulation, and by summing the results obtained at various instants of these multiplications by means of an integration-summation element 14. The signal representative of the code and subcarrier modulation has been obtained by multiplying by means of a multiplier 13, a signal representative of the code generated locally on the basis of  $\tau$ , by a signal representative of the subcarrier generated locally on the basis of  $\psi$ ,  $\tau$  and  $\psi$  respectively being the phase of the local code and of the local subcarrier, which are in fact identical in this case.

The result of this correlation is submitted to a carrier phase discriminator 15 which deduces therefrom a carrier deviation which is a real signal and which is injected into a carrier loop corrector 16. A phase calculation element 17 which may be a numerically controlled oscillator calculates the phase  $\varphi$  of the local carrier as a function of the carrier speed

emanating from the carrier loop corrector 16, and of the frequency of the carrier without Doppler effect, referred to as the carrier gauge frequency. The carrier speed is the speed of propagation of the carrier measured on reception: from this one deduces the variation in frequency of the carrier due to the Doppler effect. This phase  $\phi$  thus slaved is used by a carrier generator to generate a local carrier of the form  $e^{-i\phi}$ .

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The correlation of the signal received with the local signal is achieved likewise on a so-called delta channel (hence the notation  $I_\Delta$  and  $Q_\Delta$  for delta I channel and delta Q channel), by multiplying by means of a multiplier 21 the digitized signal multiplied by a signal of the form  $e^{-i\phi}$ , by a so-called delta signal. This delta signal emanating from a summator 20 is the difference of the signal representative of the code and carrier modulation which has undergone a lead by means of a device 18 making it possible to advance the signal with respect to that of the punctual channel and a delay by means of a device 19 making it possible to delay the signal with respect to that of the punctual channel. The results obtained at various instants of these multiplications are summed by means of an integration-summation element 22.

The result of this correlation and the result of the punctual channel is submitted to a code phase discriminator 23 which deduces therefrom a code deviation which is a real signal and which is injected into a code loop corrector 24. A phase calculation element 25 which may be a numerically controlled oscillator calculates the phases  $\tau$  and  $\psi$  of the local code and of the local subcarrier as a function of the code speed (identical to the subcarrier speed) emanating from the code loop corrector 24 and the code gauge frequency. The code speed is the speed of propagation of the code measured on reception: from

35

this we deduce the variation in code frequency due to the Doppler effect. The phases  $\tau$  and  $\psi$  of the code and of the subcarrier which are identical, are thus slaved and then respectively used by a code generator 26 to  
5 generate the local code and by a subcarrier generator 27 to generate the local subcarrier.

As these phases are identical they are calculated by the same phase calculation element 25. Represented in  
10 Figure 8 is the detail of a code phase calculation element 25. It comprises a converter 30 of the code speed expressed in m/s, into a measurement expressed in Hz of the frequency variation due to the Doppler effect, the conversion being performed on the basis of  
15 the chip of the code; the phase calculation element furthermore comprises a summator 31 of this measurement of the Doppler effect and of the code gauge frequency and an integrator 32 transforming this new frequency into a phase  $\tau$ . Represented in Figure 9a) is the local  
20 code generated by the code generator 26 as a function of the local phase expressed in chips, the chip being the wavelength of the code; Figure 9b) represents the local subcarrier generated by the subcarrier generator 27 as a function of the local phase also expressed in  
25 chips, since the same phase calculation element 25 has been used for both generators 26 and 27.

In the case of the invention, the sampling frequency used at the level of the receiver has been reduced by  
30 means of a translation towards one another of the main lobes of the spectrum of the signal received. This translation has reduced the frequency of the subcarrier which has become  $f_{\text{spread}}$ . The reduced subcarrier frequency then being different (lower) from the frequency of the  
35 code, it is therefore necessary to divorce the element for calculating the phase of the subcarrier which takes account of the reduced subcarrier frequency, from the element for calculating the phase of the code which

takes account of the frequency of the code as represented in Figure 10.

Represented in Figure 11 are the details of the phase calculation elements 25 and 28 respectively used for the code and for the subcarrier. The phase calculation element 25 used for the code is the same as that of Figure 8. The phase calculation element 28 used for the subcarrier comprises a converter 33 of the code speed (which is the same as the subcarrier speed) expressed in m/s, into a measurement expressed in Hz of the frequency variation due to the Doppler effect, the conversion being performed on the basis of the wavelength of the subcarrier expressed in cycles; the phase calculation element furthermore comprises a summator 34 of this measurement of the Doppler effect and of the reduced gauge frequency of the subcarrier and an integrator 35 transforming this new frequency into a phase  $\psi$ . It will be noted that the Doppler effect is independent of the reduction of the subcarrier frequency which intervenes only at the receiver level.

Represented in Figure 12a) is the local code generated by the code generator 26 as a function of the local phase expressed in chips; Figure 12b) represents the local subcarrier generated by the subcarrier generator 27 as a function of the local phase expressed in cycles, since a phase calculation element 28 specific to the subcarrier has been used upstream of the generator 27.

When  $f_{\text{spread}} = B/2$ , we have a chip = a cycle as represented in Figures 12 but this is no longer the case if  $f_{\text{spread}} > B/2$ .